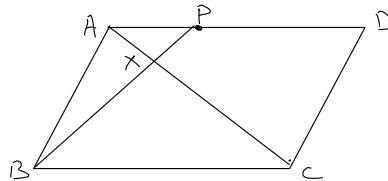


Q) ABCD is a parallelogram such that P is on AD and AP:AD = 1:P and X is the intersection of AC and BP. Prove that AX:AC = 1:(P+1)



Ans:- AP = m AD = pm
PD = (p-1)m BC = pm

In ΔAPX and ΔBCX , $\frac{CX}{AX} = \frac{BX}{PX} = \frac{BC}{AP}$

$\frac{CX}{AX} = \frac{p}{1}$ CX = CA - AX

$\Rightarrow \frac{CA - AX}{AX} = p \Rightarrow \frac{CA}{AX} = p + 1 \Rightarrow AX:AC = 1:(p+1)$

Q) Circle C_1 has its centre O lying on circle C_2 . The two circles meet at X and Y. Point Z in the exterior of C_1 lies on circle C_2 and XZ = 13, OZ = 11 and YZ = 7. What is the radius of C_1

Let r be the radius of C_1

Ans:-

OX = OY = OP = r = OQ
OM \perp XZ

$\angle XOY = \angle XOZ = \angle YOZ = \angle ZOY$

ΔOXZ

$r^2 = 13^2 + 11^2 - 2 \cdot 13 \cdot 11 \cos \alpha$ (1)

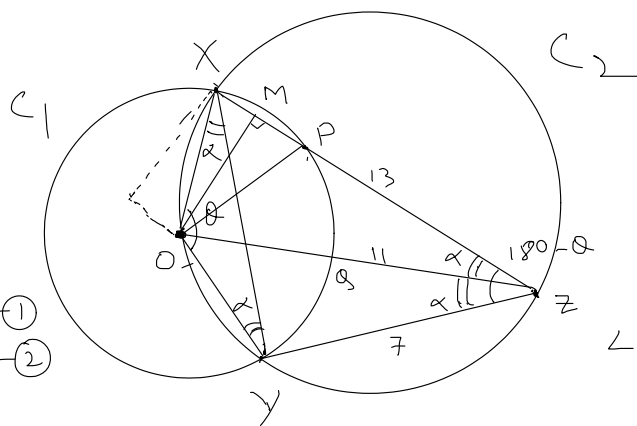
$r^2 = 11^2 + 7^2 - 2 \cdot 11 \cdot 7 \cos \alpha$ (2)

(1) \times 7 - (2) \times 13 \Rightarrow

$7r^2 - 13r^2 = 7(13^2 + 11^2) - 13(11^2 + 7^2)$

$\Rightarrow 6r^2 = 13 \times 11^2 + 13 \times 7^2 - 7 \times 13^2 - 7 \times 11^2$

$\Rightarrow r = \sqrt{\frac{180}{6}} = \sqrt{30}$



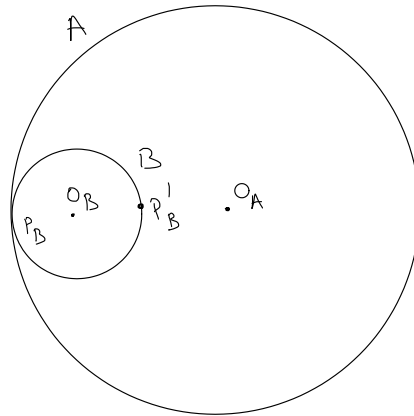
$\angle XOZ = \angle ZOY$ as $\widehat{XO} = \widehat{OY}$

Q) Circle A has radius 100, Circle B has integer radius $r < 100$ and remains internally tangent to circle A as it rolls once around circumference of circle A. The two circles have the same

and remains internally tangent to circle A. The two circles have the same points of tangency at the beginning and end of circle B's trip. How many possible values can r have?

Ans:-
 $A \rightarrow 2\pi \cdot 100$
 $B \rightarrow 2\pi r$
 $\leftarrow (2\pi r) = 2\pi \cdot 100$
 $\leftarrow k = \frac{100}{r}$
 $k \in \mathbb{Z} \quad r = 8$

$100 = 25^2$
 $(2H)(2H)$
 but what
 100 what
 included P_A



To take a full round and P_B touch with P_A integer multiple of circumference of B should roll

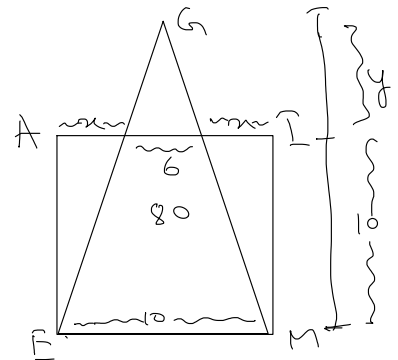
Q) Square AIME has sides of length 10 units. Isosceles triangle GEM has base EM and the area common to ΔGEM and AIME is 80 sq. units. Find the length of altitude to EM in ΔGEM .

Ans:- As common area is > 50 G must be outside square

$$x \left(\frac{1}{2} x \times 10 \right) = 20 \Rightarrow x = 2$$

$$\frac{6}{10} = \frac{y}{y+10} \Rightarrow 6y+60 = 10y \Rightarrow 4y=60 \Rightarrow y=15$$

\Rightarrow Altitude = 25



HomeWork:-

Q) Point K lies on diagonal BD of parallelogram ABCD. AK intersects lines BC and CD at L and M respectively. Prove that $AK^2 = LK \cdot KM$.

